



EUROPEAN UNION
European Structural and Investing Funds
Operational Programme Research,
Development and Education

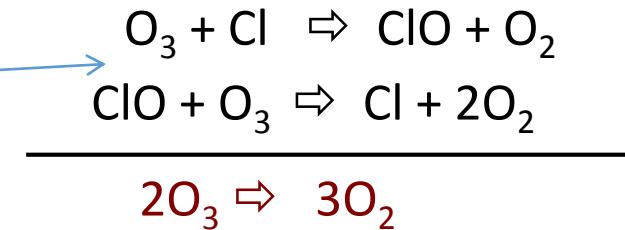


MINISTRY OF EDUCATION,
YOUTH AND SPORTS

9. Kinetics of catalytic reactions

• homogeneous catalysis

- Ozone decomposition in the presence of Cl
- SO₂ oxidation by NO_x
- Esterification catalyzed by acids or bases
- Enzymatic catalysis

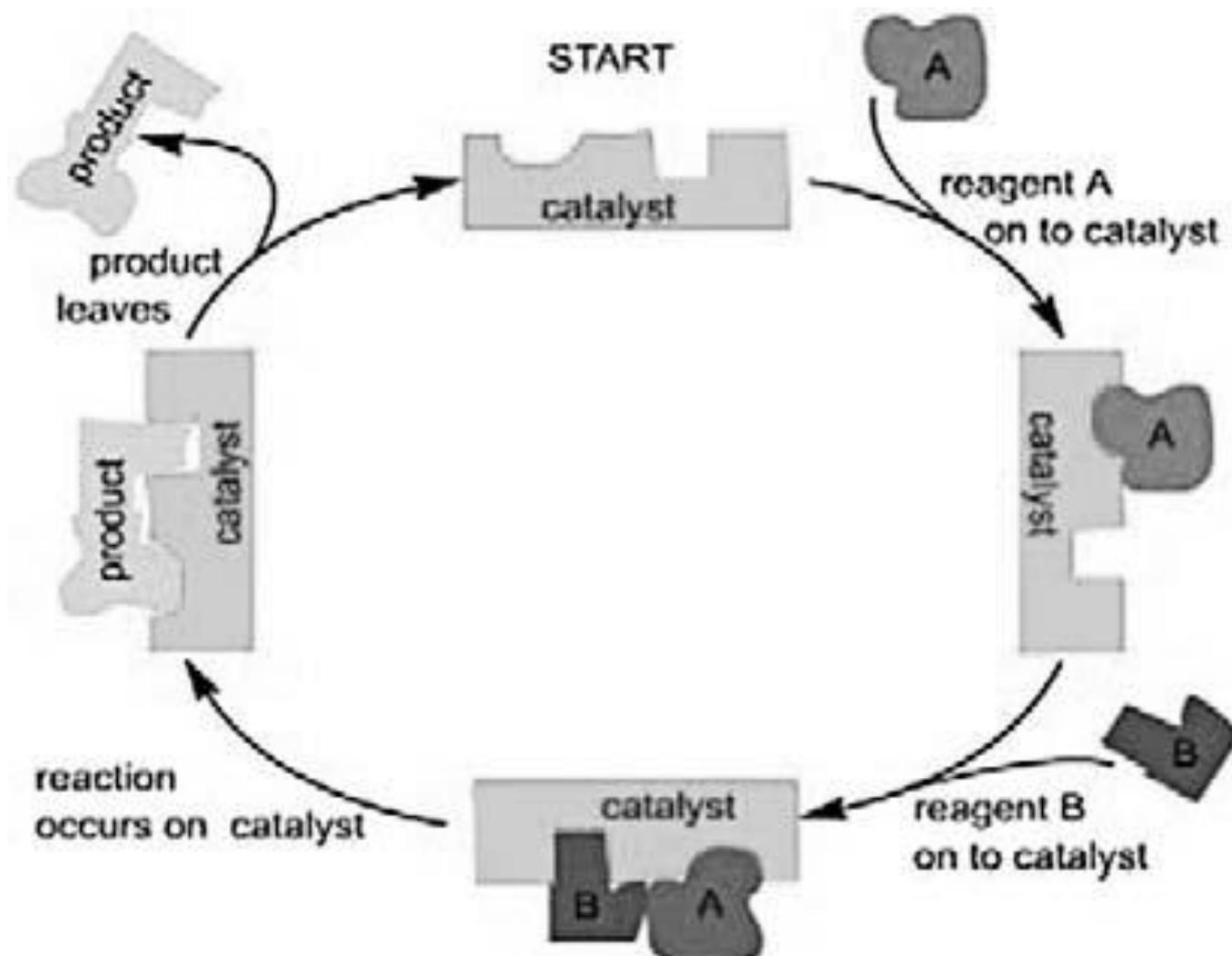


• heterogeneous catalysis

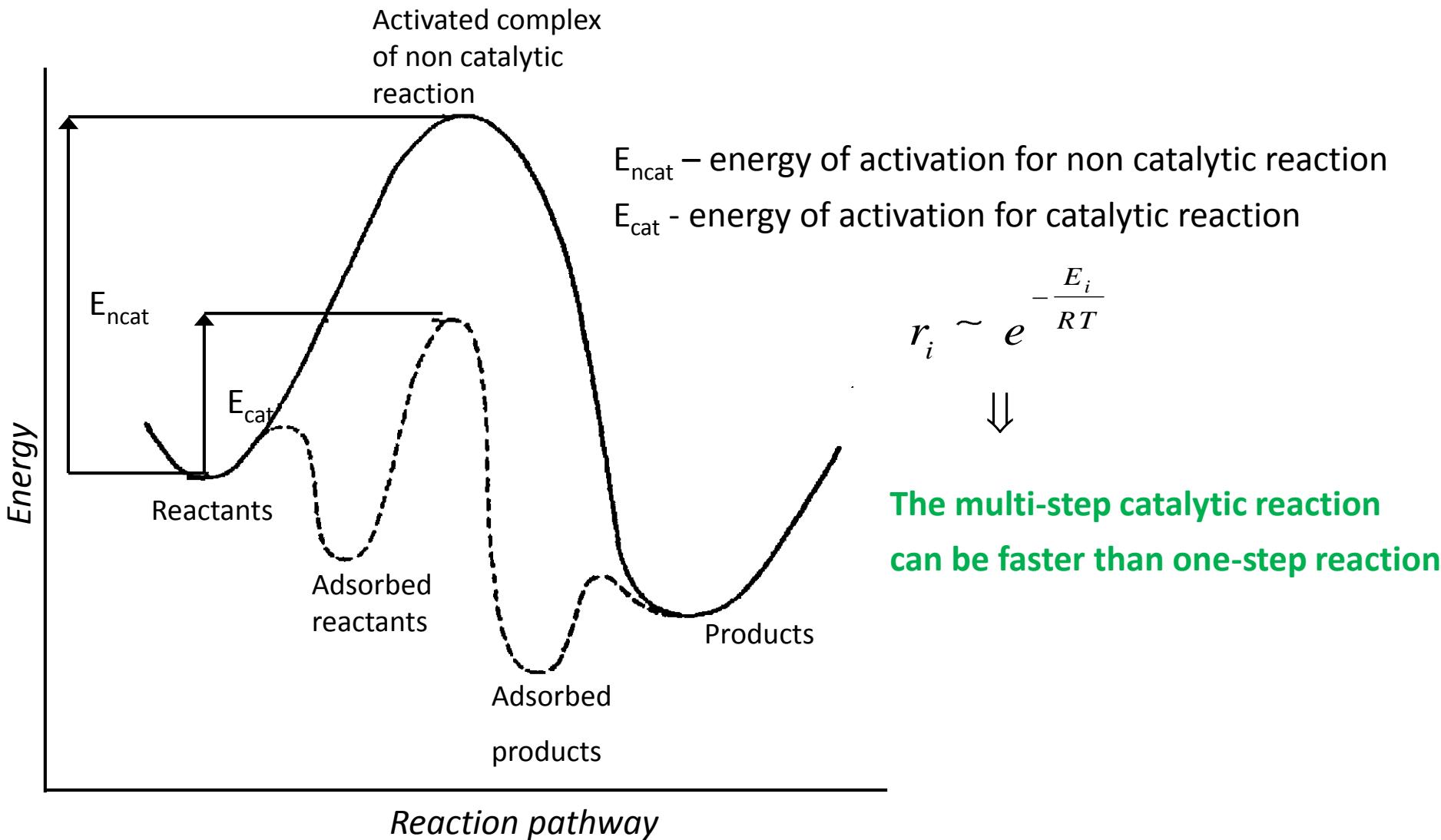
- NH₃, CH₃OH production
- SO₂ to SO₃ oxidation
- HDS, HDN processes
- Fluid Catalytic Cracking
- Hydrogenation
- Polymerization (Ziegler-Natta catalysts, metallocens)



Catalytic cycle



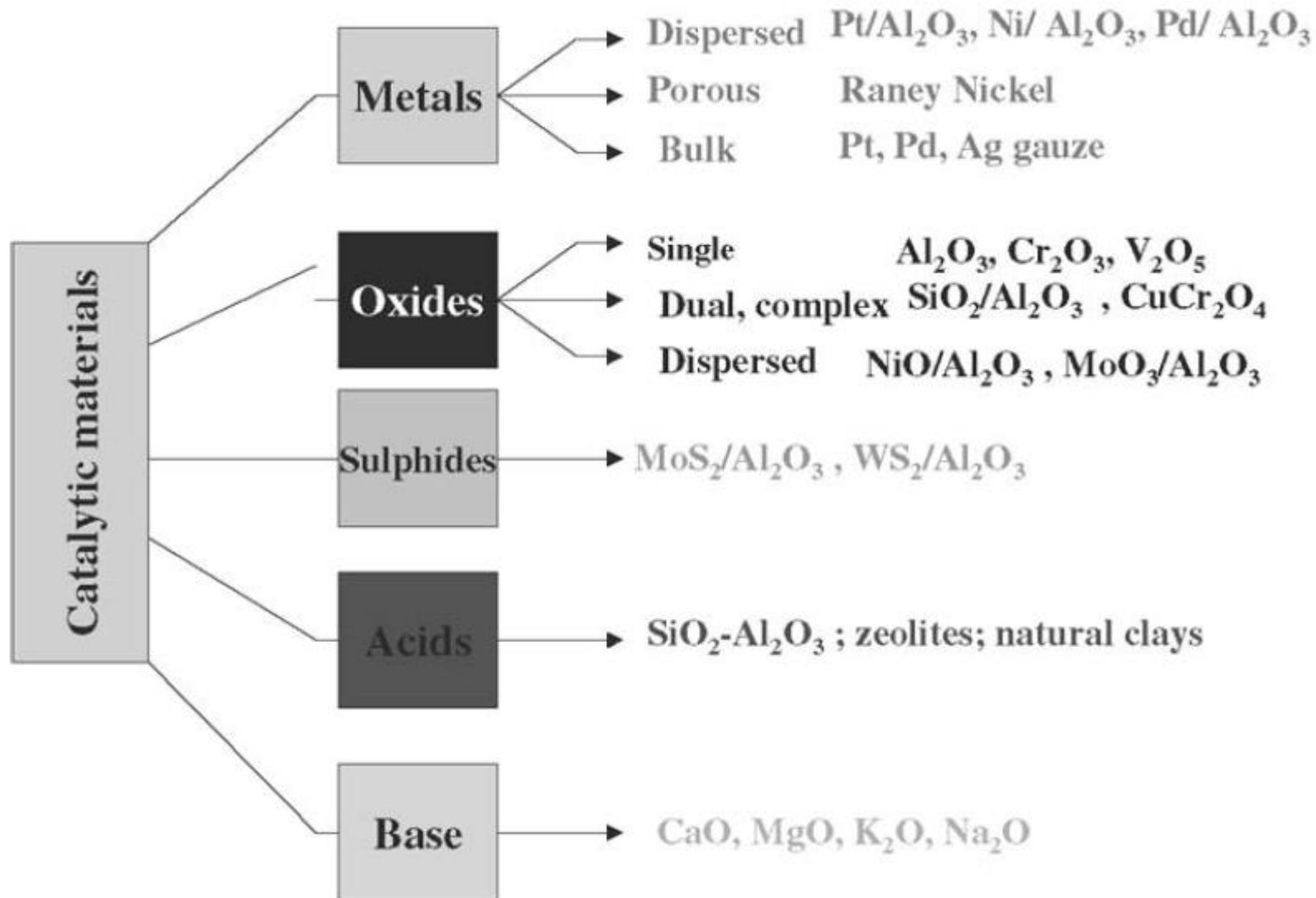
Non catalytic x catalytic reaction



Homogeneous x Heterogeneous Catalysts

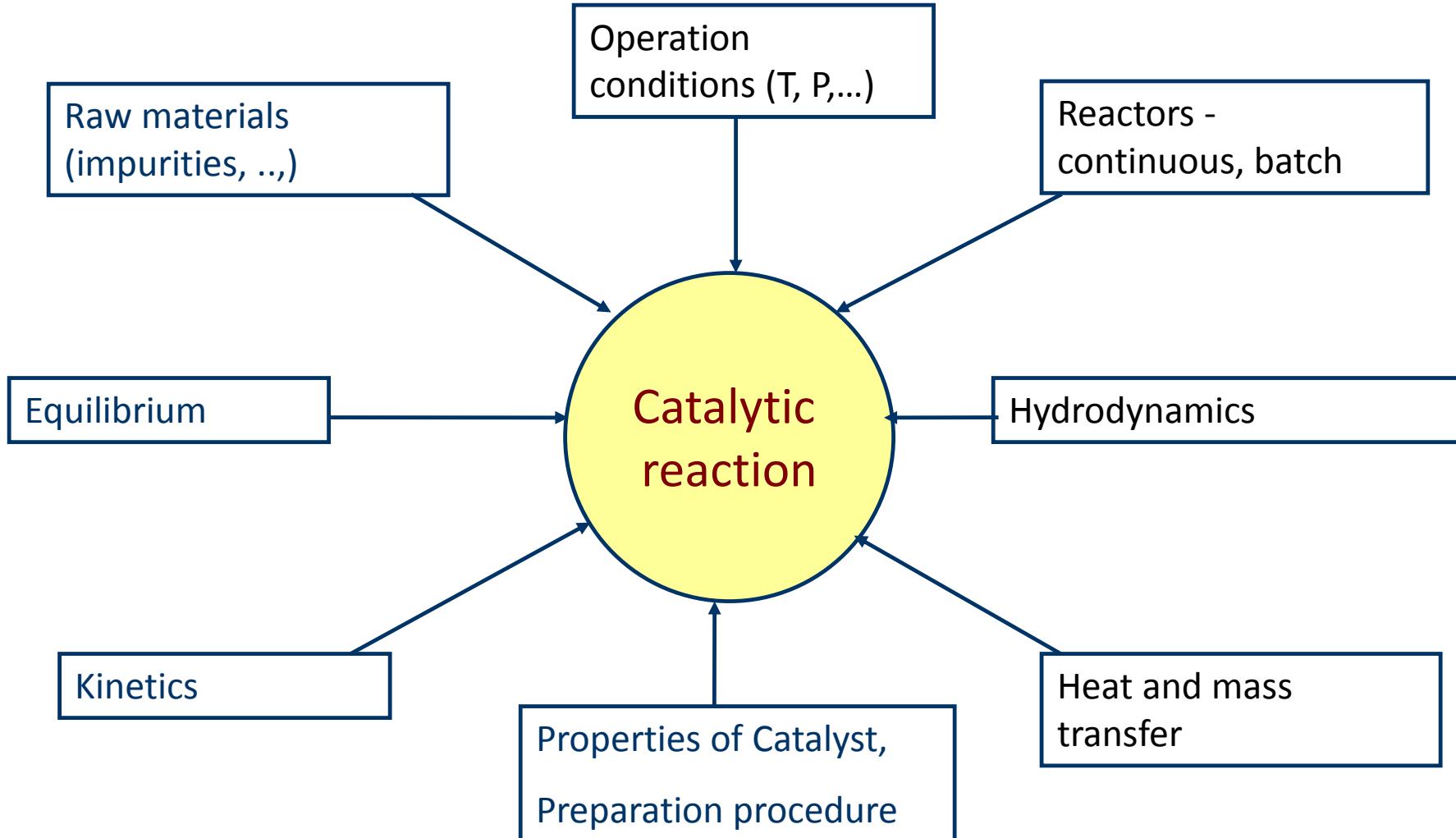
		<i>Homogeneous</i>	<i>Heterogeneous</i>
<i>Active sites</i>	Concentration	All atoms	Surface atoms
	Diffusion disguises	No	Low
	Reaction conditions		High (variable)
	Application		Important
		50-200 °C	200-1000 °C
<i>Characterization</i>	Structure, composition	Well defined	No clear definition
	Modification	Easy	Difficult
	Temperature stability	Low	High
<i>Separation</i>		Difficult	Easy packed beds
<i>Recycling</i>		Feasible	Feasible

Reactant(s)	Product	Typical catalyst(s)	Global Production/t year ⁻¹
Crude oil	Hydrocarbon fuels	Platinum/silica-alumina Platinum/acidic alumina Metal-exchanged zeolites	1*10 ⁹
SO ₂ , O ₂	Sulphuric acid	V ₂ O ₅	1.4*10 ⁸
N ₂ , H ₂	Ammonia	Fe	9*10 ⁷
NH ₃ , O ₂	Nitric acid	Pt/Rh	2.5* 10 ⁷
CO, H ₂	Methanol	Cu/ZnO	1.5*10 ⁷
C ₂ H ₄ , O ₂	Ethylene oxide	Ag	1*10 ⁷
Unsaturated vegetable oils, H ₂	Hydrogenated vegetable oils	Ni	8*10 ⁶
C ₂ H ₄	Polyethylene	Cr(II), Ti(III)	6*10 ⁶
CH ₃ OH, O ₂	Formaldehyde	Mixed Fe, Mo oxides	5*10 ⁶
C ₃ H ₆ , NH ₃ , O ₂	Acrylonitrile	Mixed Bi, Mo oxides	3*10 ⁶
o-Xylene, O ₂	Phthalic anhydride	V ₂ O ₅	4*10 ⁶
n-Butane, O ₂	Maleic anhydride	V ₂ O ₅	4*10 ⁵



Catalyst	Reaction
Metals (e.g., Ni, Pd, Pt, as powders or on supports) or metal oxides (e.g., Cr ₂ O ₃)	C=C bond hydrogenation, e.g., olefin + H ₂ → paraffin
Metals (e.g., Cu, Ni, Pt)	C=O bond hydrogenation, e.g., acetone + H ₂ → isopropanol
Metal (e.g., Pd, Pt)	Complete oxidation of hydrocarbons, oxidation of CO
Fe (supported and promoted with alkali metals)	3H ₂ + N ₂ → 2NH ₃
Ni	CO + 3H ₂ → CH ₄ + H ₂ O (methanation)
Fe or Co (supported and promoted with alkali metals)	CO + H ₂ → paraffins + olefins + H ₂ O + CO ₂ (+ other oxygen-containing organic compounds) (Fischer-Tropsch reaction)
Cu (supported on ZnO, with other components, e.g., Al ₂ O ₃)	CO + 2H ₂ → CH ₃ OH
Re + Pt (supported on η -Al ₂ O ₃ or γ -Al ₂ O ₃ promoted with chloride)	Paraffin dehydrogenation, isomerization and dehydrocyclization

Catalyst	Reaction
Solid acids (e.g., SiO ₂ -Al ₂ O ₃ , zeolites)	Paraffin cracking and isomerization
γ -Al ₂ O ₃	Alcohol → olefin + H ₂ O
Pd supported on acidic zeolite	Paraffin hydrocracking
Metal-oxide-supported complexes of Cr, Ti or Zr	Olefin polymerization, e.g., ethylene → polyethylene
Metal-oxide-supported oxides of W or Re	Olefin metathesis, e.g., 2 propylene → ethylene + butene
Ag(on inert support, promoted by alkali metals)	Ethylene + 1/2 O ₂ → ethylene oxide (with CO ₂ + H ₂ O)
V ₂ O ₅ or Pt	2 SO ₂ + O ₂ → 2 SO ₃
V ₂ O ₅ (on metal oxide support)	Naphthalene + 9/2O ₂ → phthalic anhydride + 2CO ₂ + 2H ₂ O
Bismuth molybdate	Propylene + 1/2O ₂ → acrolein
Mixed oxides of Fe and Mo	CH ₃ OH + O ₂ → formaldehyde (with CO ₂ + H ₂ O)
Fe ₃ O ₄ or metal sulfides	H ₂ O + CO → H ₂ + CO ₂

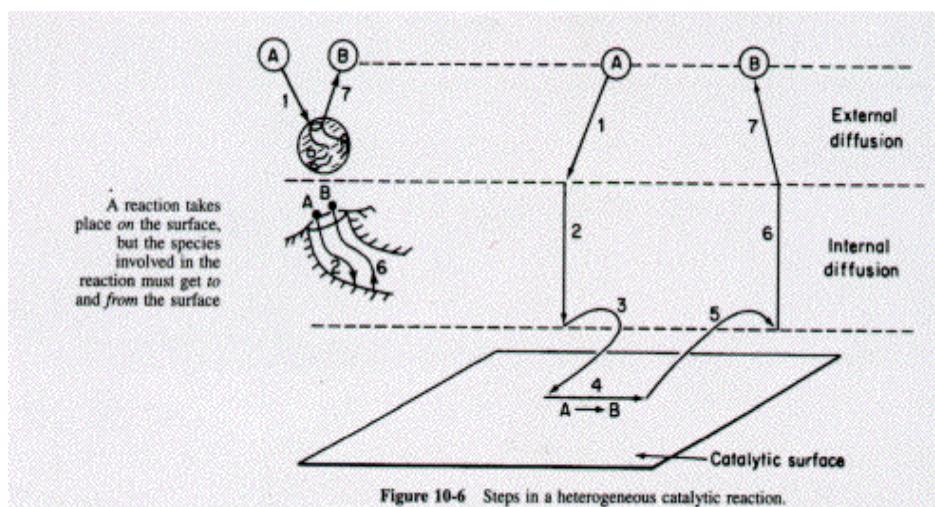


Steps in a catalytic reaction

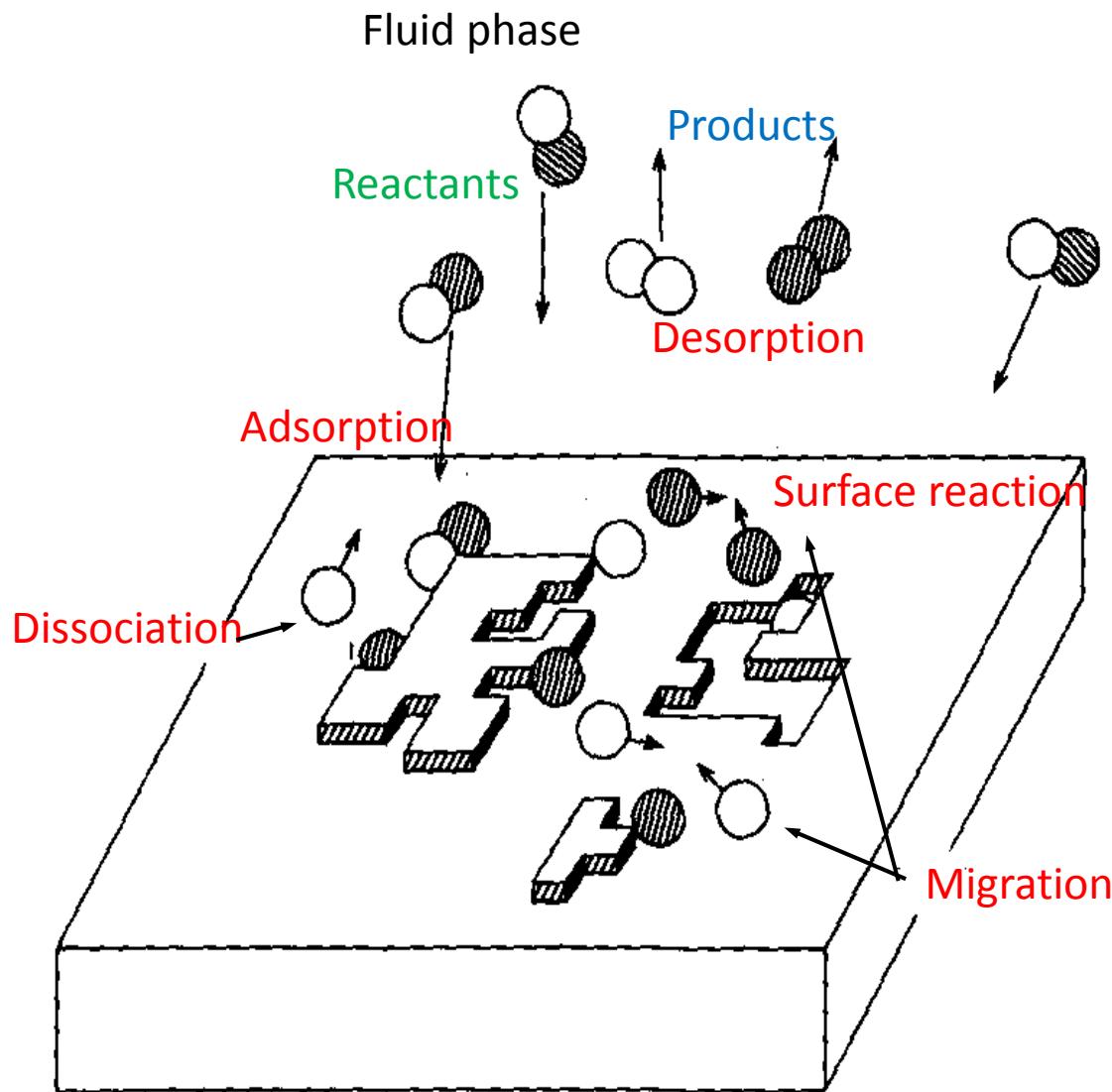
- 1) Mass transfer of reactants to the external surface of catalyst
- 2) Mass transfer of reactants in porous structure of catalyst
- 3) *Adsorption of reactants*
- 4) *Surface reaction (+ migration)*
- 5) *Desorption of products*
- 6) Mass transfer of products in porous structure of catalyst
- 7) Mass transfer of reactants from the external surface of catalyst

The transport steps (1,2,6,7) depend on T, P, composition, flow rates, pore size,

The chemical steps (3,4,5) are dependent on T, P, composition.

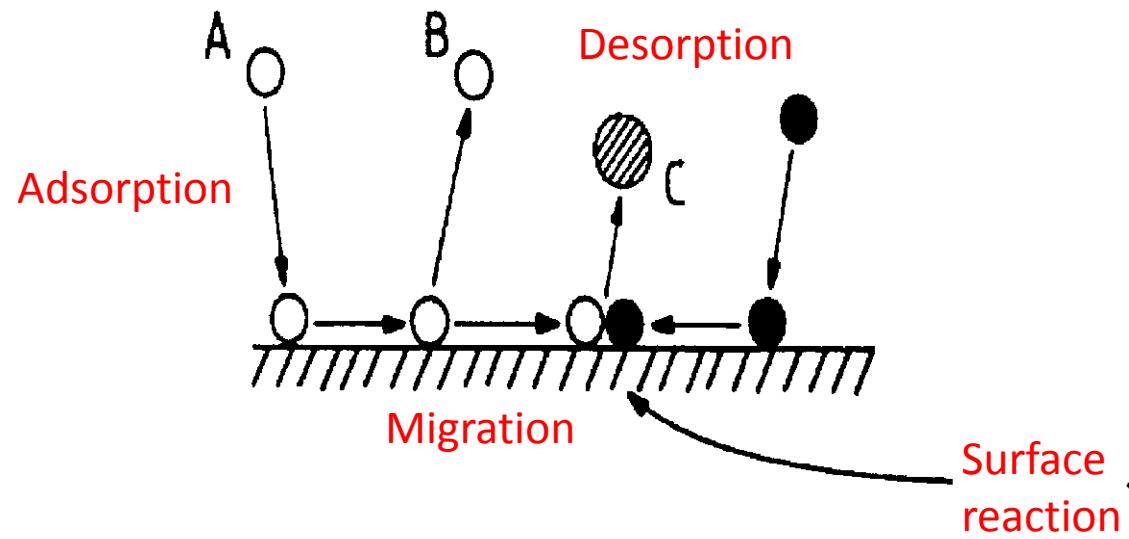


Elementary steps of catalytic reaction

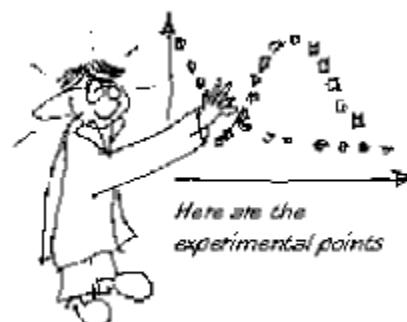
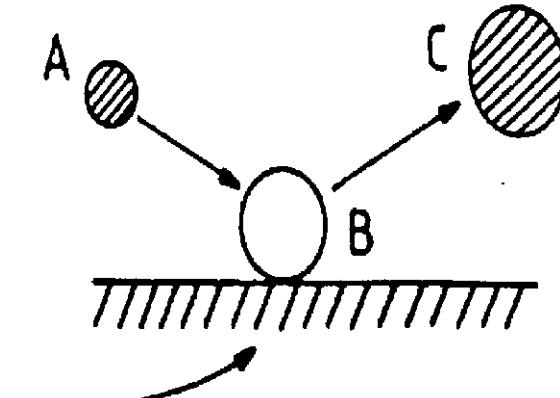


Mechanisms in heterogeneous catalysis

Langmuir-Hinshelwood



Rideal-Eley

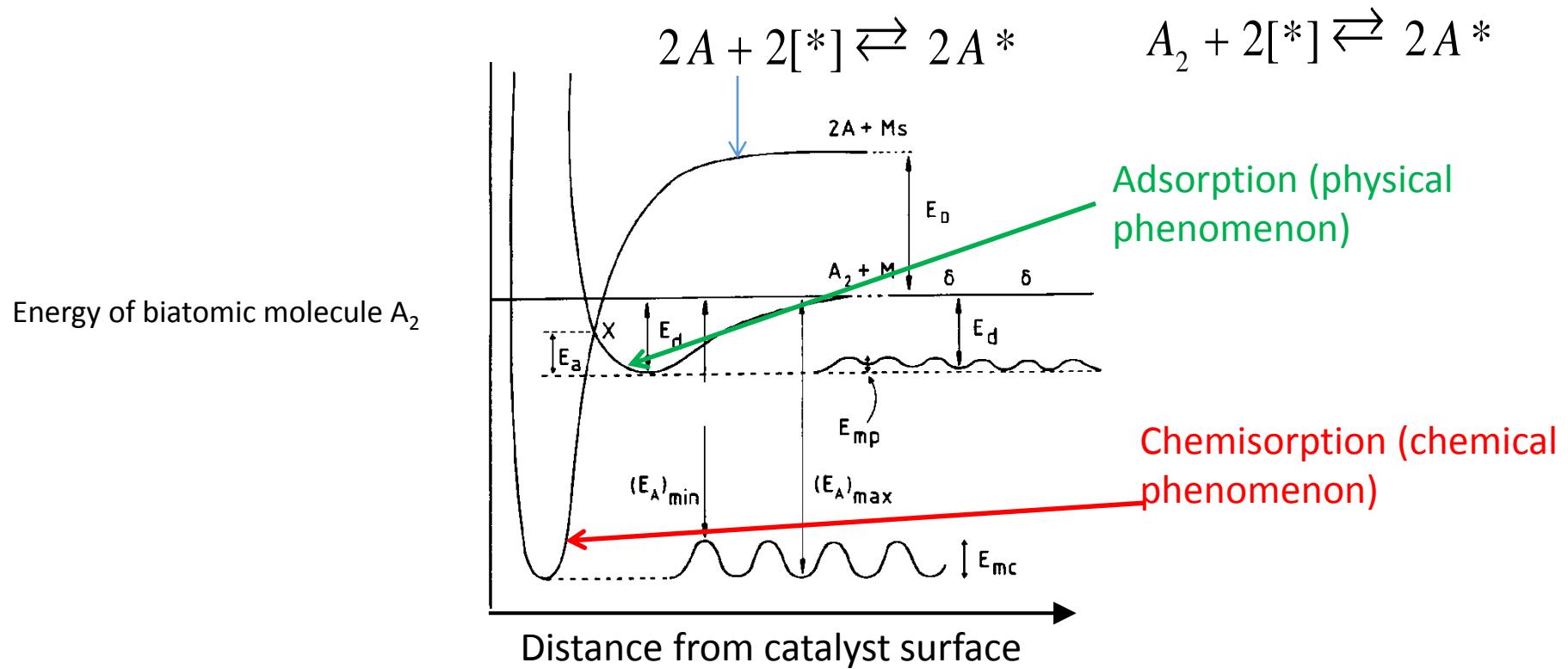


$$r = \frac{k_{A,B} c_A c_B}{(1 + k_{H,H} c_H + k_{N,N} c_N)^2}$$

Here is the kinetic model

A cartoon scientist is pointing at a complex mathematical equation representing the kinetic model.

Adsorption x Chemisorption



E_{mc}, E_{mp} – activation energy of migration in adsorbed and chemisorbed state

E_D – energy of dissociation of molecule A_2

E_d – energy of desorption of A_2

E_a – energy of activation of transition from adsorbed to chemisorbed state

Adsorption x Chemisorption

	<i>Adsorption</i>	<i>Chemisorption</i>
Principal	van der Waals forces no electron transfer !	covalent or ionic bonds electron transfer
Adsorbent	all solids	specific sites
Adsorbat	gases $T < T_c$	reactive components
Temperature	low	higher
Enthalpy	10-40 kJ/mol	80-600 kJ/mol
Rate	high	depends on T
Activation energy	low	high
Occupancy	multilayer	monolayer
Reversibility	YES	YES but ...
Use	BET method pore size distribution	surface concentration of active sites

Chemisorption of fluid phase molecule (adsorbat)

Surface occupancy(Θ)

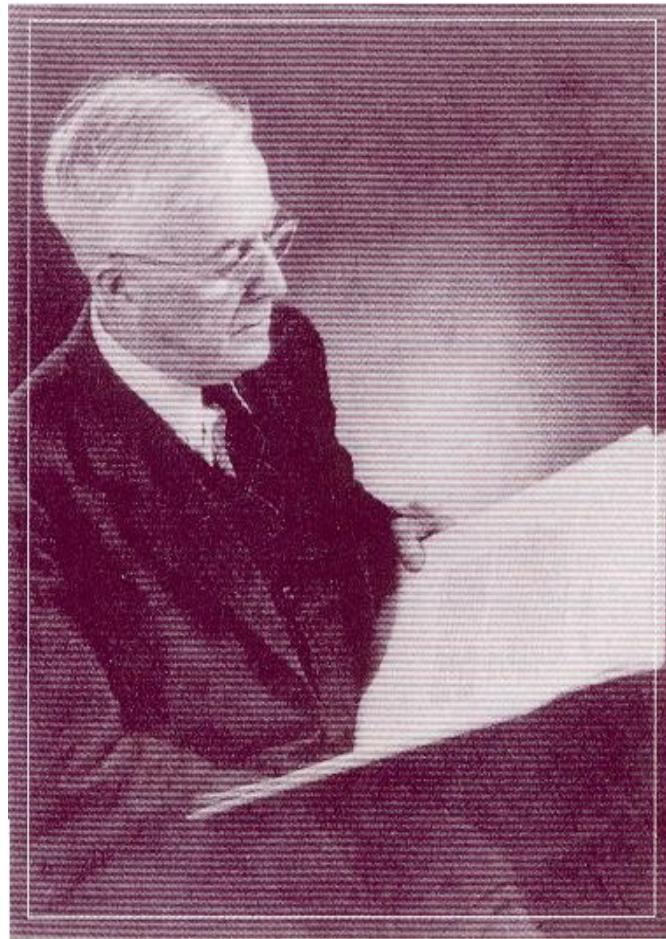
$$\Theta_i = \frac{\text{Number of sites occupied by } i\text{-th component}}{\text{Total number of sites}}$$
$$0 < \Theta_i < 1$$

Associative x Dissociative chemisorption

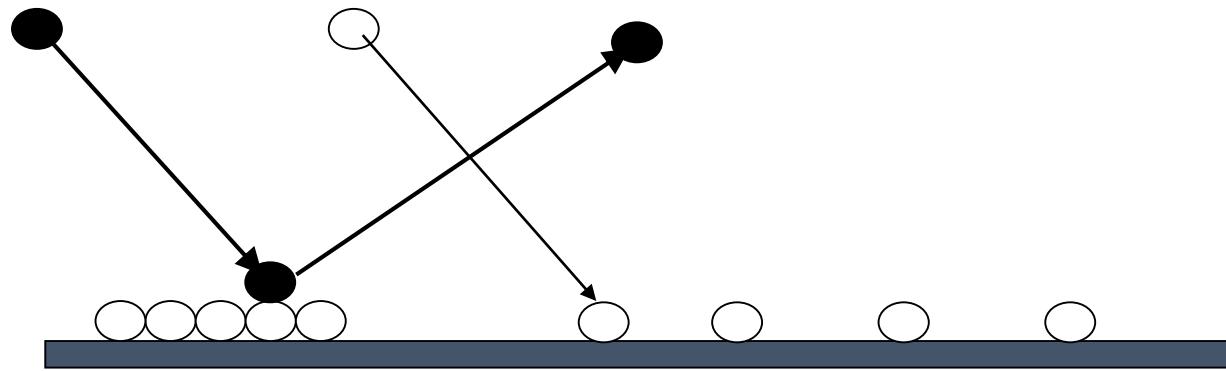
Adsorption (chemisorption) isotherm – Surface occupancy as a function of partial pressure of given component at constant temperature

Irving Langmuir

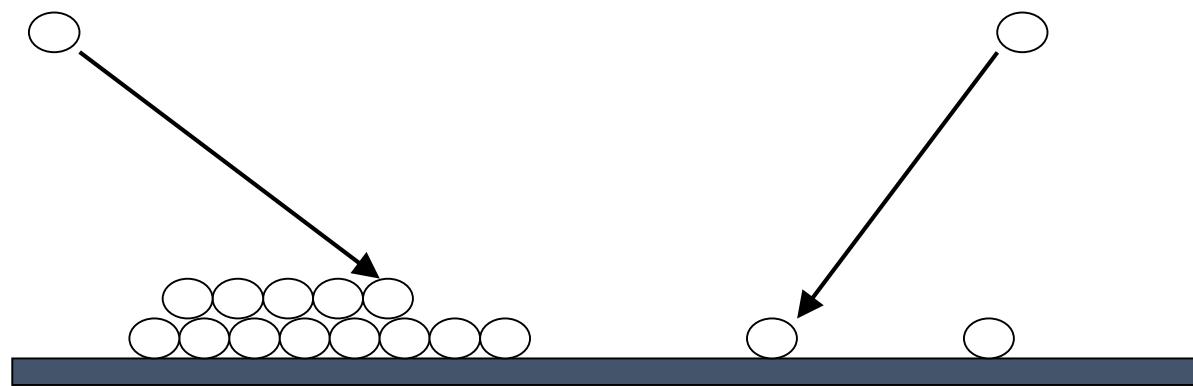
- 1920 - adsorption isotherm
 - kinetics of catalytic reactions
 on ideal surfaces
- 1932 - Nobel Prize



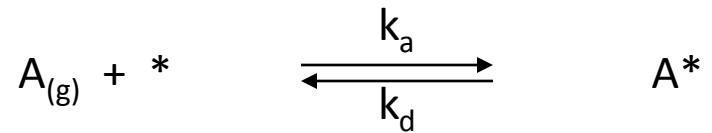
Langmuir adsorption isotherm



Brunauer-Emmett-Teller (BET) adsorption isotherm



Associative adsorption on ideal catalytic surface



$$\text{Rate of chemisorption} = k_a \cdot P_A \cdot (1 - \Theta_A)$$

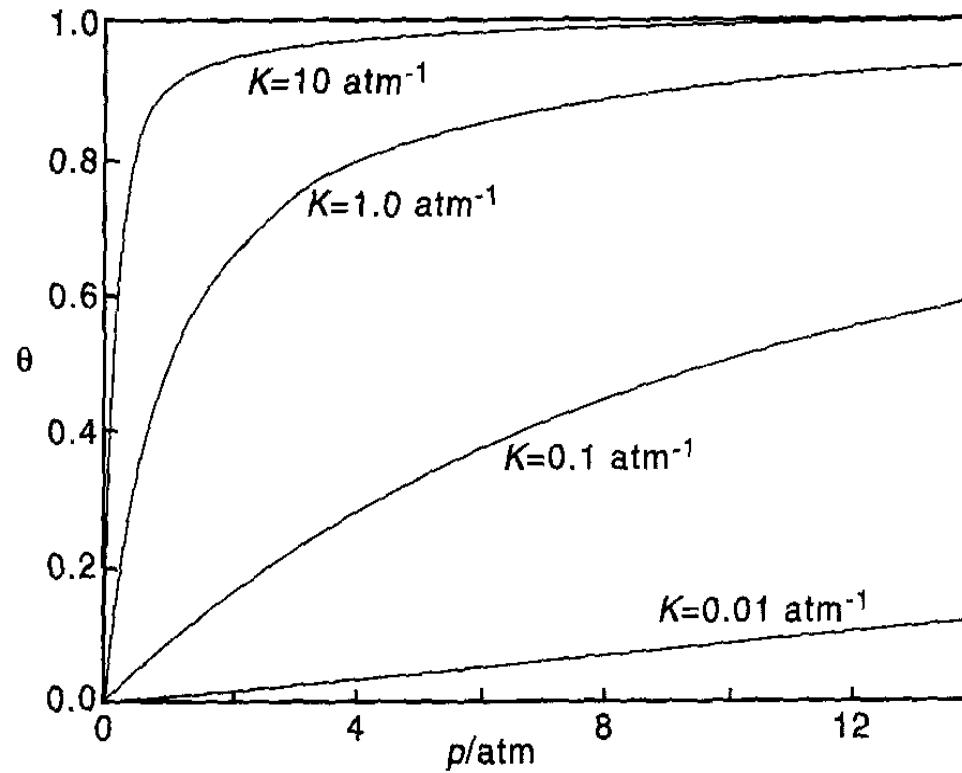
$$\text{Rate of desorption} = k_d \cdot \Theta_A$$

At equilibrium

$$k_a \cdot p \cdot (1 - \Theta_A) = k_d \cdot \Theta_A \quad (K_A = k_a/k_d)$$

$$\frac{\Theta_A}{(1 - \Theta_A)} = K_A \cdot P_A \quad \Rightarrow \quad \Theta_A = \frac{K_A P_A}{1 + K_A P_A}$$

Asociative chemisorption



Langmuir adsorption (chemisorption) isotherm

Multicomponent associative chemisorption on ideal catalytic surface



Occupancy of A

$$\Theta_A = \frac{K_A \cdot p_A}{1 + K_A \cdot p_A + K_B \cdot p_B}$$

Occupancy of B

$$\Theta_B = \frac{K_B \cdot p_B}{1 + K_A \cdot p_A + K_B \cdot p_B}$$

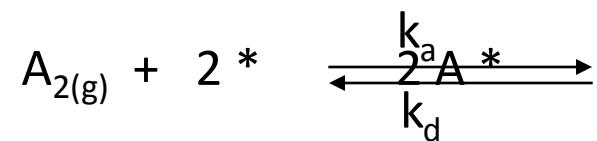
$$K_A = k_a / k_d$$

$$K_B = k_b / k_d$$

Irreversible chemisorption

 catalyst poisoning

Dissociative chemisorption on ideal catalytic surface



$$\text{Rate of chemisorption} = k_a \cdot P_A \cdot (1 - \Theta_A)^2$$

$$\text{Rate of desorption} = k_d \cdot \Theta_A^2$$

At equilibrium

$$k_a \cdot p \cdot (1 - \Theta_A)^2 = k_d \cdot \Theta_A^2 \quad (K_A = k_a/k_d)$$

$$\frac{\Theta_A^2}{(1 - \Theta_A)^2} = K_A \cdot P_A \quad \Rightarrow \quad \Theta_A = \frac{\sqrt{K_A P_A}}{1 + \sqrt{K_A P_A}}$$

Isotherms

Langmuir

(chemisorption, adsorption,
monolayer, micropores)

$$\frac{(n_A)_{adsorbed}}{(n_*)} = \Theta_A = \frac{K_A P_A}{1 + K_A P_A}$$

Henry

(chemisorption, adsorption, low occupancy)

$$\frac{(n_A)_{adsorbed}}{(n_*)} = \Theta_A = K_A P_A$$

Freundlich

(chemisorption, adsorption, non ideal)

$$\frac{(n_A)_{adsorbed}}{(n_*)} = \Theta_A = K_A (P_A)^{\frac{1}{n}}$$

Temkin

(chemisorption, non ideal)

$$\frac{(n_A)_{adsorbed}}{(n_*)} = \Theta_A = \alpha_A \ln(\beta_A P_A)$$

Brunauer-Emmett-Teller (BET)

(adsorption, multilayer)

$$\frac{P_A}{(n_A)_{ads}(P_A^o - P_A)} = \frac{1}{n_m C} + \frac{(C-1)}{n_m C} \frac{P_A}{P_A^o}$$

Virial

(adsorption, multilayer)

$$\frac{P_A}{R.T} = \Theta_A (1 + a_1 \Theta_A + a_2 \Theta_A^2 + \dots)$$

Brunauer-Emmett-Teller (BET)

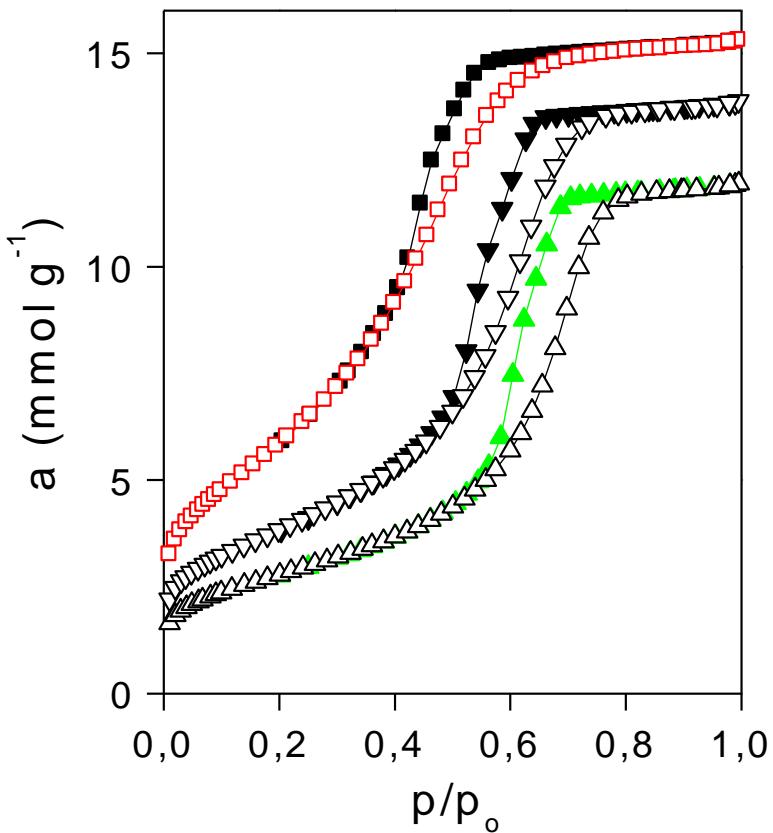
Extention of Langmuir model

Assumptions:

- adsorption in multilayer s, 1st layer interaction between adsorbent and adsorbat, in 2nd and further layers condensation-like interaction

$$\frac{P_A}{(n_A)_{ads} (P_A^o - P_A)} = \frac{1}{n_m C} + \frac{(C-1)}{n_m C} \frac{P_A}{P_A^o}$$

Mesoporous alumina



Temperature od calcination : 3,3 nm (450 °C) - 4,5 nm (600 °C) - 5,1 nm (800 °C)

Reaction rate per mass

$$r_M = \frac{1}{m} r = \frac{1}{m} \frac{d\xi}{dt} = \frac{1}{m} \frac{1}{\nu_i} \frac{dn_i}{dt} \quad \text{mole.kg}^{-1}.s^{-1}$$

$$r_{M,k} = \frac{1}{m} r_k = \frac{1}{m} \frac{d\xi_k}{dt}$$

Reaction rate per surface

$$r_S = \frac{1}{S} r = \frac{1}{S} \frac{d\xi}{dt} = \frac{1}{S} \frac{1}{\nu_i} \frac{dn_i}{dt} \quad \text{mole.m}^{-2}.s^{-1}$$

$$r_{S,k} = \frac{1}{S} r_k = \frac{1}{S} \frac{d\xi_k}{dt}$$

Reaction rate per active center (turnover number)

$$r_{RS} = \frac{1}{n_{RS}} r = \frac{1}{n_{RS}} \frac{d\xi}{dt} = \frac{1}{n_{RS}} \frac{1}{\nu_i} \frac{dn_i}{dt} \quad \text{s}^{-1}$$

$$r_{RS,k} = \frac{1}{n_{RS}} r_k = \frac{1}{n_{RS}} \frac{d\xi_k}{dt}$$

Reaction rate of catalytic reactions

Langmuir-Hishelwood ideal surface

- ◎ Rate of elementary steps
- ◎ Rate determining step x steady state hypothesis

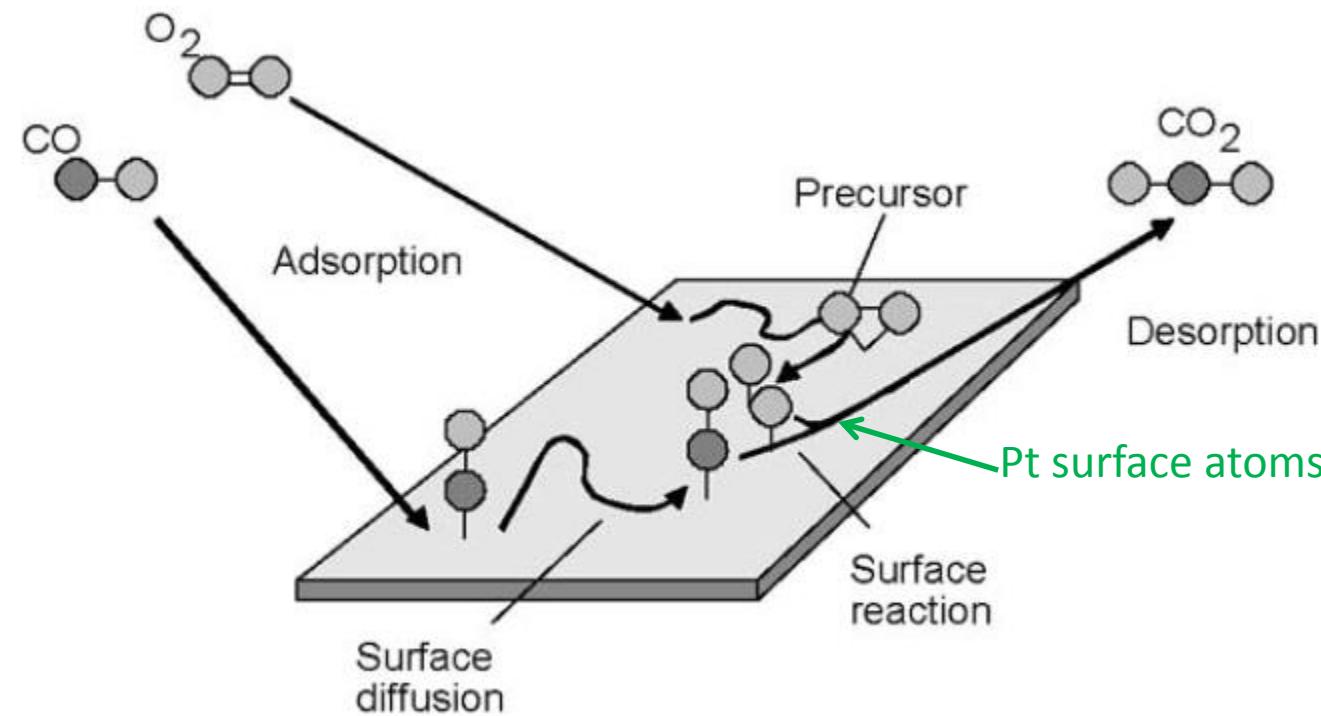
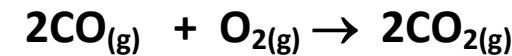
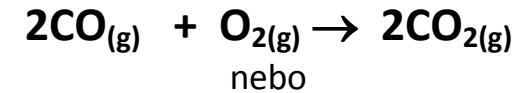
Reaction rate of catalytic reactions

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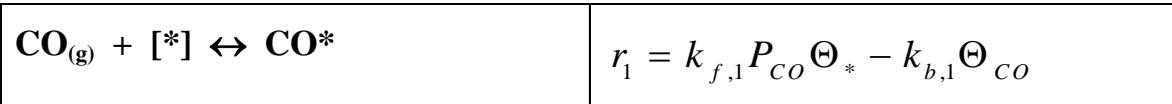
CO oxidation on Pt

Overall reaction ($\Delta G_r^{\circ} < 0$)



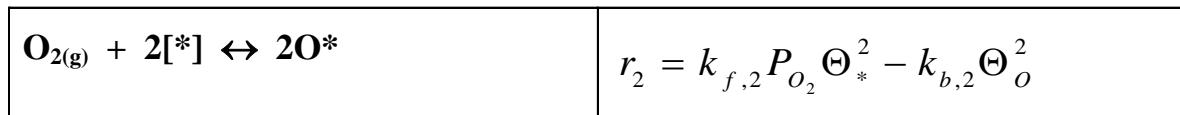
Elementary steps of catalytic CO oxidation on Pt

1. CO chemisorption

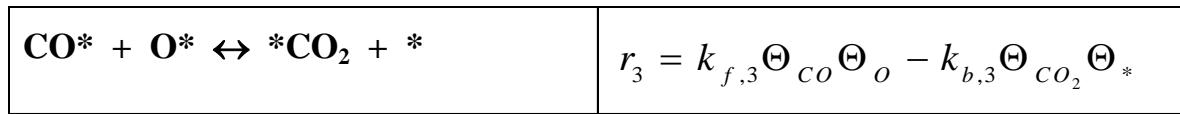


2. O₂ dissociative chemisorption

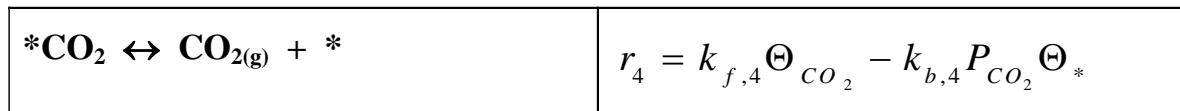
* - Pt surface atoms = Catalytic active centre



3. Surface reaction between CO* and O*



4. CO₂ desorption into gas phase



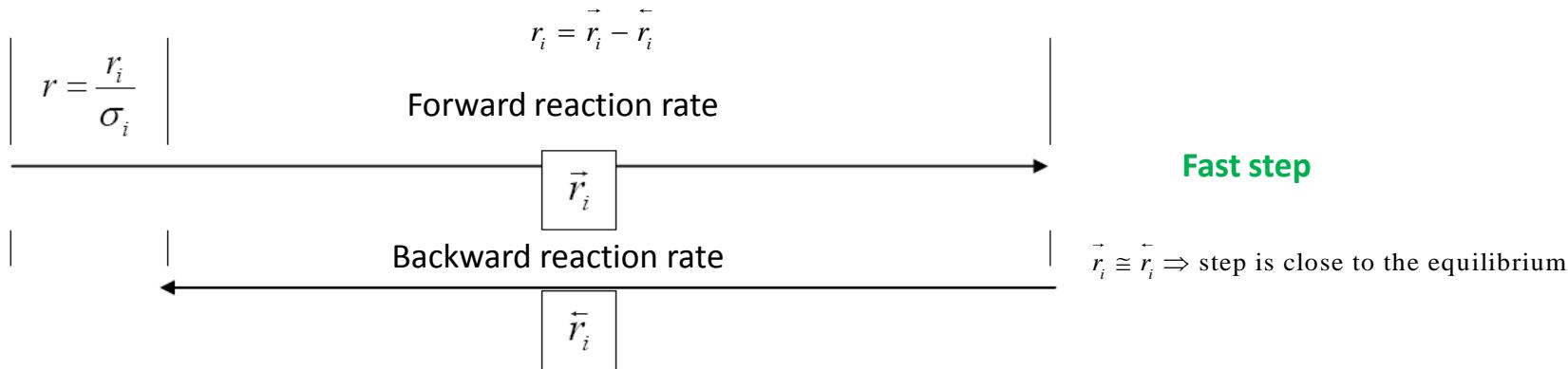
P_i – partial pressures of gaseous components [Pa]

Θ_i - occupancy (coverage) of the i-th species [-]

$k_{f,j}, k_{b,j}$ - reaction rate constants

r_j – rate of the j-th elementary step [mol/kg katalyzátoru/s
mol/molPt/s= 1/s]

Rate determining step in steady state



Relation between overall reaction rate and the rate of i-th elementary step determines the stoichiometric number σ_i
 (do not confuse with stoichiometric coefficient !)

$$r = \frac{r_i}{\sigma_i}$$

	σ_i
$\text{CO}_{(\text{g})} + [*] \leftrightarrow \text{CO}^*$	2
$\text{O}_{2(\text{g})} + 2[*] \leftrightarrow 2\text{O}^*$	1
$\text{CO}^* + \text{O}^* \leftrightarrow * \text{CO}_2 + *$	2
$* \text{CO}_2 \leftrightarrow \text{CO}_{(\text{g})} + *$	2
$2\text{CO}_{(\text{g})} + \text{O}_{2(\text{g})} \rightarrow 2\text{CO}_{2(\text{g})}$	

M. Boudart, 1968, in “Kinetics of Chemical Processes”:

The stoichiometric number of i-th elementary step, σ is the number of times that this elementary step, as written, must be repeated, in the closed sequence, in order to obtain by summation of all steps the overall stoichiometric equation for reaction, as written.

Rate determining step: surface reaction

$$K_{CO} = \frac{k_{f,1}}{k_{b,1}} = \frac{\Theta_{CO}}{P_{CO}\Theta_*} \quad K_{O_2} = \frac{k_{f,2}}{k_{b,2}} = \frac{\Theta_O^2}{P_{O_2}\Theta_*^2} \quad K_{CO_2} = \frac{k_{b,4}}{k_{f,4}} = \frac{\Theta_{CO_2}}{P_{CO_2}\Theta_*}$$

$$\Theta_* + \Theta_{CO} + \Theta_O + \Theta_{CO_2} = 1$$

$$\Theta_* = \frac{1}{1 + K_{CO}P_{CO} + \sqrt{K_{O_2}P_{O_2}} + K_{CO_2}P_{CO_2}}$$

$$\Theta_{CO} = \frac{K_{CO}P_{CO}}{1 + K_{CO}P_{CO} + \sqrt{K_{O_2}P_{O_2}} + K_{CO_2}P_{CO_2}}$$

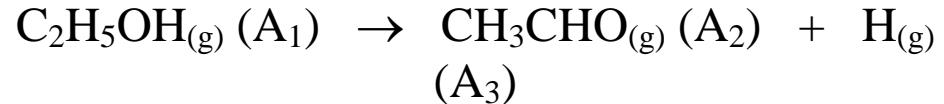
$$\Theta_O = \frac{\sqrt{K_{O_2}P_{O_2}}}{1 + K_{CO}P_{CO} + \sqrt{K_{O_2}P_{O_2}} + K_{CO_2}P_{CO_2}}$$

$$\Theta_{CO_2} = \frac{K_{CO_2}P_{CO_2}}{1 + K_{CO}P_{CO} + \sqrt{K_{O_2}P_{O_2}} + K_{CO_2}P_{CO_2}}$$

Reaction rate as a function of measurable variables

$$r_3 = k_{f,3}\Theta_{CO}\Theta_O - k_{b,3}\Theta_{CO_2}\Theta_* = \frac{k_{f,3}K_{CO}\sqrt{K_{O_2}}P_{CO}\sqrt{P_{O_2}} - k_{b,3}K_{CO_2}P_{CO_2}}{\left[1 + K_{CO}P_{CO} + \sqrt{K_{O_2}P_{O_2}} + K_{CO_2}P_{CO_2}\right]^2}$$

Example



catalysts: CuO, CoO a Cr₂O₃

(Franckaerts J., Froment G.F., Kinetic study of the dehydrogenation of ethanol, Chem. Eng. Sci. 19 (1964) 807-818).

Kinetics

$$r_M = \frac{k K_1 \left(P_1 - P_2 P_3 / K_{eq} \right)}{\left(1 + K_1 P_1 + K_2 P_2 \right)^2}$$

r_M (mol.g⁻¹.hod⁻¹), P_i (bar), k (mol.g⁻¹.hod⁻¹), K_{eq} (bar), K_i (bar⁻¹).

Task: to estimate on the basis of experimental data kinetic and adsorption parameters k, K_1, K_2

EXPERIMENTAL SET-UP

Franckaerts J., Froment G.F., Kinetic study of the dehydrogenation of ethanol, Chem. Eng. Sci. 19 (1964) 807-818

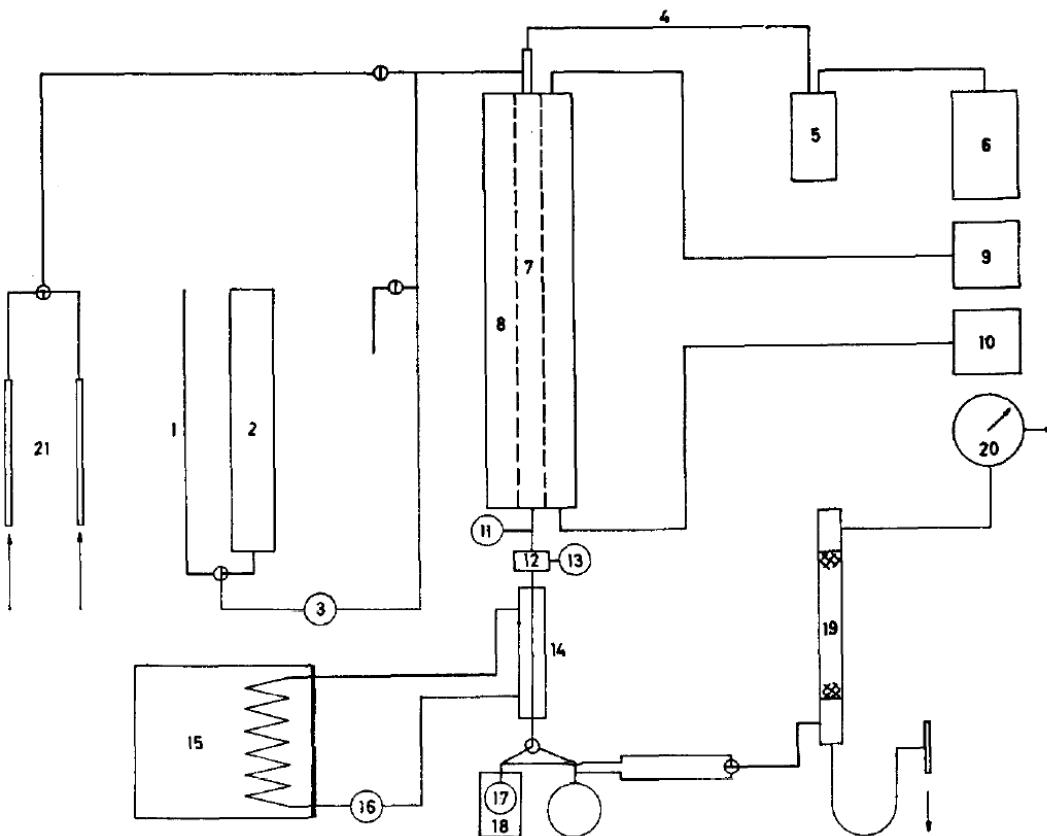


FIG. 1. Apparatus: 1,2, feed burettes; 3, metering pump; 4, thermocouples; 5, ice-bath; 6, mV-recorder; 7, reactor; 8, reactor-mantle; 9,10, variable transformers; 11,13, manometers; 12, pressure regulating device; 14, cooler; 15, cooling unit; 16, circulating pump; 17, sampling flask; 18, liquid air trap; 19, saturator, eventually also absorber in periods between sampling; 20, wet test meter; 21, flowmeters for air and nitrogen.

EXPERIMENTAL DATA

W / F_1^o [g.hod/mol]	P [bar]	y_1^o [-]	y_4^o [-]	y_2^o [-]	T [°C]	X_1 [-]
1,60	7,0	0,865	0,135	0,0	225,0	0,066
0,80	4,0	0,865	0,135	0,0	225,0	0,083
0,40	3,0	0,865	0,135	0,0	225,0	0,055
1,0	1,0	0,865	0,135	0,0	225,0	0,118
1,0	1,0	0,750	0,130	0,119	225,0	0,052
0,40	1,0	0,865	0,135	0,0	225,0	0,060
1,0	1,0	0,732	0,167	0,101	225,0	0,052
0,40	10,0	0,865	0,135	0,0	225,0	0,038
1,60	7,0	0,865	0,135	0,0	250,0	0,149
0,80	4,0	0,865	0,135	0,0	250,0	0,157
0,40	3,0	0,865	0,135	0,0	250,0	0,108
1,0	1,0	0,865	0,135	0,0	250,0	0,218
1,0	1,0	0,672	0,145	0,183	250,0	0,123
0,60	1,0	0,865	0,135	0,0	250,0	0,152
0,80	1,0	0,672	0,145	0,183	250,0	0,106
0,60	10,0	0,865	0,135	0,0	250,0	0,094
1,60	7,0	0,865	0,135	0,0	275,0	0,254
0,80	4,0	0,865	0,135	0,0	275,0	0,262
0,40	3,0	0,865	0,135	0,0	275,0	0,20
1,0	1,0	0,865	0,135	0,0	275,0	0,362
1,0	1,0	0,672	0,145	0,183	275,0	0,230
0,20	1,0	0,865	0,135	0,0	275,0	0,118
0,40	10,0	0,865	0,135	0,0	275,0	0,148
0,40	1,0	0,865	0,135	0,0	275,0	0,196

Solution:

Minimize the objective function:

$$\Phi(k, K_1, K_2) = \sum_{i=1}^{NEXP} \left[X_{1,i}^{\text{exp}} - X_{1,i}^{\text{mod}}(k, K_1, K_2) \right]^2$$

$X_{1,i}^{\text{mod}}(k, K_1, K_2)$ calculated from isothermal catalytic PFR model:

$$\frac{dX_1}{d(W / F_1^o)} = r_M(X_1) \quad W / F_1^o = 0, X_1 = 0$$

ATHENA Visual Studio.

Priklad_9_1.avw - Athena Visual Studio

File Edit Model Build View Format Tools VisualKinetics Windows Help

Priklad_9_1.avw

```
! Catalytic Ethanol Dehydrogenation Kinetics
!-----
Global k1,Ka1,Ka2,Ka3,Ka4 As Real
Global TEMP, Press, Ymol(3) As Real

@Connect Variables
k1 =Par(1) ! Reaction rate constant
Ka1=Par(2) ! Adsorption equilibrium constant for ethanol
Ka2=Par(3) ! Adsorption equilibrium constant for acetaldehyde
Ka3=Par(4) ! Adsorption equilibrium constant for hydrogen
Ka4=Par(5) ! Adsorption equilibrium constant for water
TEMP = Xu(6) + 273.15D0 ! Temperature [K]
Press = Xu(2) ! Pressure [atm]
Ymol(1) = Xu(3) ! Feed ethanol mol. fraction
Ymol(2) = Xu(4) ! Feed water mol. fraction
Ymol(3) = Xu(5) ! Feed acetaldehyde mol. fraction

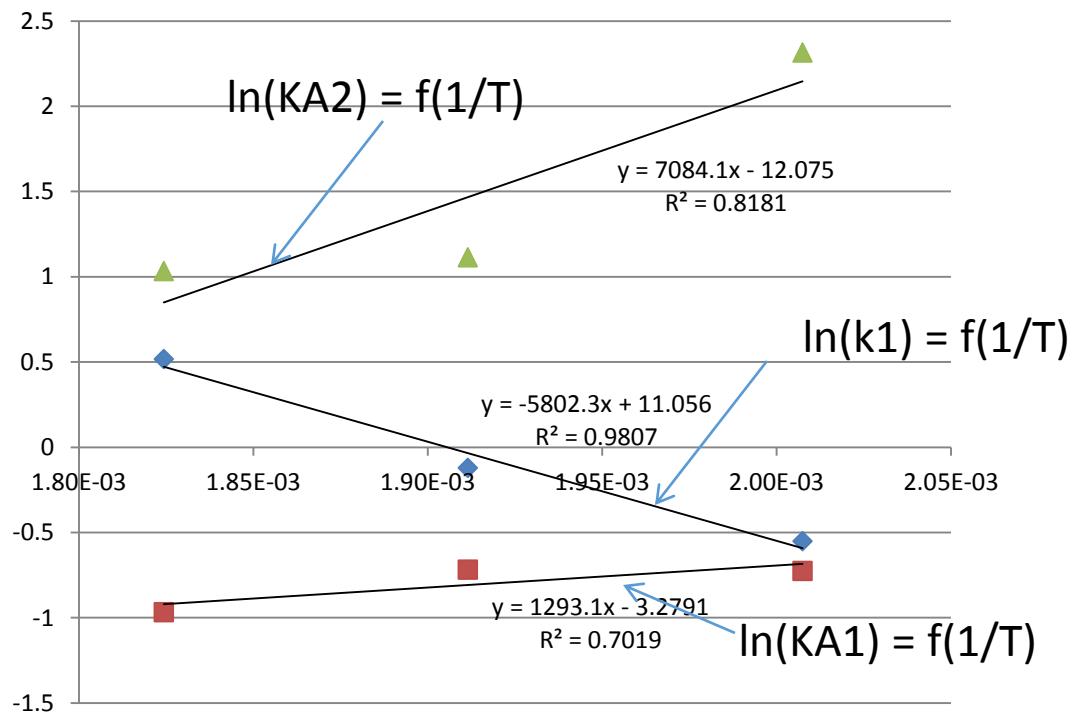
@Initial Conditions
U(1)=0.0

@Model Equations
Dim PA1, PA2, PA3, PA4, KEQ, X1, RR, AUX As Real
KEQ = DEXP(-14159.9D0/TEMP+25.2681D0)
X1 = U(1)
AUX = (1.0D0+Ymol(1)*X1)/Press
PA1 = Ymol(1)*(1.0D0-X1)/AUX ! Ethanol partial pressure
PA2 = (Ymol(3)+Ymol(1)*X1)/AUX ! Acetaldehyde partial pressure
PA3 = Ymol(1)*X1/AUX ! Hydrogen partial pressure
PA4 = Ymol(2)/AUX ! Water partial pressure
RR = k1*(PA1-PA2*PA3/KEQ)/(1.0D0+Ka1*PA1+Ka2*PA2+Ka3*PA3+Ka4*PA4)^2
F(1) = RR

@Response Model
Y(1)=U(1)
```

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	225 oC	250 oC	275 oC
k1	5.767986E-01 +- 4.112E-01	8.863130E-01 +- 1.668E-01	1.675828E+00 +- 4.225E-01
KA1	4.839934E-01 +- 3.591E-01	4.876108E-01 +- 9.443E-02	3.803293E-01 +- 1.473E-01
KA2	1.011693E+01 +- 7.376E+00	3.044445E+00 +- 9.054E-01	2.812096E+00 +- 1.078E+00



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